# An Analysis for Optimization of Rubber Granule Layer in Synthetic Surfaced Track using Response Surface Methodology

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# 반응표면법을 이용한 육상트랙용 고무칩층의 최적설계에 관한 연구

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Abstract This paper aims to evaluate the effect of each material ingredient on mechanical and dynamic performance and to determine an optimal mixing condition of a rubber granule layer. To minimize the required number of tests, the test matrix was established by using the design of experiments (DOE). The tensile tests were then performed to identify the mechanical properties. Also, to evaluate the dynamic performance that the IAAF has required for athletics tracks for athletes' safety and balance, a series of impact tests were performed by using the so-called the "artificial athlete" machine. Finally, the response surface methodology was used to decide the optimal mixing conditions needed to achieve a high level of mechanical properties and dynamic performance.

**요 약** 본 논문은 육상트랙용 복합탄성포장재의 고무칩층의 최적 배합조건을 결정하기 위하여 기계적 및 동적 성능 에 대한 각 구성요소의 영향을 평가한 것이다. 이에 소요되는 시험 횟수의 최소화를 위하여 실험계획법을 적용하였으 며 이에 따라 기계적 및 국제육상연맹(IAAF)에서 요구하는 동적성능에 대한 시험을 수행하였다. 마지막으로 반응표면 법을 이용하여 기계적 특성 및 동적 성능을 최적화하기 위한 배합조건을 결정하였다.

Key Words : Dynamic Performance, Optimization, Response Surface Methodology, Rubber Granule Layer

### 1. Introduction

Modern synthetic surfaces are high performance systems formulated to be durable and designed to offer the best combination of dynamic performance. These have been widely used through the world for their dynamic performance, durability and all-weather capability for athletic tracks [1-3]. There are several sub-division of surface type: some are prefabricated in factories and delivered to sites as rolls of material that are bonded to the base; some (in-situ system) are fabricated on site by machine mixing and laying the raw material ingredients; and others are composites of these two systems [1].

In Korea, the elastic compound pavement system which is a kind of in-situ system, has been most commonly used for the outdoor tracks for public use [4]. The system is formed from a base layer of resin-bound rubber granule. After curing, a polyurethane layer is applied to form the top surface. Among these layers, the granule layer is a mixture of rubber granule with a polyurethane resin in the correct proportion and plays an important role in the dynamic performance and durability of the surface. There are a considerable number of installers [4] and, unfortunately, they have used different

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rubber granules and resins, even varying the mixing proportions. Moreover, the compatibility of the raw material ingredients is of vital importance and the end properties of such systems depend on the nature of the raw materials and their mixing condition.

And these surfacing systems should meet the requirements of durability and performance. Mechanical properties are most important factor for structural integrity, including durability. And since sports injuries may be associated with the dynamic performance of surfaces which is the interaction between the foot and surface [5,6], these properties are the most important factors [6]. Several researchers including the IAAF (International Amateur Athletic Federation) have revealed that the foot-surface interaction is a very complex behavior and the interaction has the extent of the variation in loading and duration of load [1,5,6]. Nevertheless, the IAAF has stipulated the dynamic performance of surfaces in terms of force reduction and vertical deformation in an attempt to assess the potential of sports surfaces to reduce the forces acting on the human body. The performance of surfacing systems, however, is affected by the nature of raw materials and their mixing condition as mentioned above. It is, therefore, necessary to decide the optimal mixing condition for the superior mechanical and dynamic performance of the rubber granule layer.

This paper examines the effect of each material ingredient on the mechanical and dynamic performance and determines an optimal mixing condition for rubber granule layers. To minimize the required number of tests, a test matrix was established by using the design of experiments (DOE). From the results of tensile and impact tests, the compatibility of the raw material ingredients was evaluated. Also, the response surface methodology was used to decide the optimal mixing condition needed to achieve a high level of mechanical and dynamic performance.

# 2. Experimental Procedure

#### 2.1 Materials and specimen

The rubber granule layer is a sub-part of the elastic compound pavement system, as shown in Fig. 1. The

layer is composed of rubber granules and a one-component moisture-curing polyurethane resin [4], as illustrated in Fig. 2. The granule was made from the three types of EPDM (ethylene propylene dien polyMethylene) and one SBR (styrene-butadiene rubber). The polyurethane resins were provided by six manufacturers in Korea. Some of the manufacturers are certified by the IAAF for the athlete tracks.



[Fig. 1] Elastic compound pavement system



[Fig. 2] Rubber granule

The layers were fabricated according to the manufacturers' recommended process with dimension of  $500 \times 500 \times 15$  mm (L×W×T). Firstly, the granules and resin were mixed very carefully according to the prescribed weight proportions and the mixed layers were cured in the environmental chamber under a temperature of  $30\pm1$ °C and relative humidity of  $60\pm5\%$  for 48 hours. And, the layers were cured under the ambient condition for 168 hours. The layers were cut into specimens with dimensions of  $180\times30\times15$ mm and  $500\times500\times15$ mm for tensile and dynamic tests, respectively.

#### 2.2 Mechanical and dynamic tests

The tensile tests were conducted at ambient temperature by using a servo-hydraulic testing machine (Instron 8801). The static tests were performed under a displacement control mode with a crosshead speed of  $50\pm0.5$ mm/min and the elongation was monitored by using an extensometer with a gage length of 50mm, according to KS M6518 [7]. Seven tensile tests were

performed for each test set.

And the dynamic performance was measured by using the in-house designed "Artificial athlete" according to the IAAF regulation [1], as shown in Fig. 3. To measure the force reduction, the foot is fitted with a force transducer that enables the peak force during the impact event to be recorded. Simultaneously, the deformation of the test foot is measured by displacement transducer mounted on both sides of the foot. The force reduction and vertical deformation were measured five and three times for each test set, respectively.



[Fig. 3] Artificial athlete

# 3. Results and Discussion

#### 3.1 Mechanical and dynamic behavior

Since the synthetic surfaces require a considerable financial investment, the quality of the synthetic surfaces should be improved with respect to their durability and sports-related performance of surface. In particular, the rubber granule layer is bounded by polyurethane resin; hence, the compatibility of the raw material ingredients is of vital importance. For this, the mechanical and dynamic tests were performed for the rubber granule layers. Here the rubber granules were supplied by three EPDM and one SBR granules manufacturers in Korea; the polyurethane resins are provided major by six manufactures. Accordingly, twenty-four layers were fabricated according to the manufacturers' recommended process, and the tensile and dynamic tests were performed for each test set.

To understand the mechanical behavior, the averaged mechanical properties are plotted against the rubber granule types in Fig. 4.



[Fig. 4] Mechanical properties of rubber granule layer

As shown in Fig. 4(a), the tensile strength is greatly affected by rubber granule types and for a given granule type, the resin is also a governing factor on the tensile strength. For example, the layer with resin type B has the highest value for all the rubber granules, while the layer with resin type C has an adverse tendency. Also, the tensile strength for a given resin type shows remarkable variation according to the rubber granule type. These behaviors may result from the adhesive characteristics between the granule and resin. Also, the failure strain in Fig. 4(b) exhibits a similar tendency.





(b) Vertical Deformation

[Fig. 5] Dynamic performance of rubber granule layer

The dynamic performance is one of the most important quantities for synthetic surfaces [5,6] and is most commonly quantified using the Artificial Athlete described in the IAAF regulation [1]. This test has been developed to simulate the initial impact force with a time and magnitude of force corresponding to those occurring in running. Fig. 5 represents the averaged dynamic performance namely, the force reduction and vertical deformation for each type of the granules. Compared with the mechanical properties, the force reduction in Fig. 5(a) is not particularly sensitive to the rubber granule and the resin type. Similar behavior could be found for the vertical deformation illustrated in Fig. 5(b). Since the load is the in-plane condition for the tensile tests, the adhesive characteristics between the granule and resin are dominating factor for improving the mechanical properties. The loads in the dynamic tests are, however, applied to the layers under out-of-plane conditions and the resin may play a role in holding the granules; hence, the properties of the rubber granules are the important factors in the dynamic performance of the surface.

#### 3.2 Optimization for performance

# 3.2.1 Design of experiments and response surface methodology

The mechanical and dynamic performance may be

associated with the durability and occurrence of surface-related injuries. Also, they may be affected by several variables related to the rubber granule laver. Based on the installers' recommendations for the variables, the authors are concerned with three design variables from mixing conditions. Table 1 and Table 2 show the design variables and their ranges, respectively according to the DOE (central composite design) [8, 9]. Here, the design variables  $x_1$ ,  $x_2$  and  $x_3$  indicate the type of polyurethane resin, the proportion of resin and the mesh distribution of the granules, respectively. Their ranges have been selected to cover the general circumstances on site in Korea. The levels of coded design variables  $x_1$  and  $x_2$  signify the polyurethane resin types (resin A-E) and the proportion of resin to the granule layer in weight. Also, the third variable  $x_3$ , mesh distribution, is the size of the rubber granules. Here the rubber granule used was the EPDM A for Fig. 4 and 5.

Basically, in the response surface methodology, an experimental model of the response should first be established, and then the fitted surface models are optimized simultaneously in a region of interest. Typical second-order models for the response are given by

$$\mu = \beta_0 + \sum_{i=1}^{k} \beta_i x_i + \sum_{i < j}^{k} \beta_{ij} x_i x_j$$
(1)

in which m is the estimated value of the responses  $(m_1$ : tensile strength,  $m_2$  : failure strain,  $m_3$  : force reduction and  $m_4$  : vertical deformation). Also, k and b are number of design variables and coefficients of the fitted response surface, respectively.

Based on the experimental results for mechanical and dynamic performance according to the central composite design, the response surfaces were fitted by using Eq. (1) and the non-linear regression method [8] as shown in Table 3. The ANOVA results for the response surfaces are summarized in Table 4. From the table, the response surfaces are statistically significant to 90% confidence

[Table	1]	Design	variables	of	rubber	granule	layer
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Factor	Factor range	-1.287	-1	0	+1	+1.287
$x_1$	Resin type	Resin A	Resin B	Resin C	Resin D	Resin E
$x_2$	Rubber proportion	16.57%	18.00%	23.00%	28.00%	29.44%
<i>x</i> <sub>3</sub>	Mesh distribution	53.91%	57.50%	70.00%	82.5%	86.09%

Series No.		Natural design	variables	variables Coded desi		
	$x_1$	$x_2$	<i>x</i> <sub>3</sub>	$x_1$	$x_2$	<i>x</i> <sub>3</sub>
1	Resin B	18.00%	57.50%	-1	-1	-1
2	Resin B	18.00%	82.50%	-1	-1	1
3	Resin B	28.00%	57.50%	-1	1	-1
4	Resin B	28.00%	82.50%	-1	1	1
5	Resin D	18.00%	57.50%	1	-1	-1
6	Resin D	18.00%	82.50%	1	-1	1
7	Resin D	28.00%	57.50%	1	1	-1
8	Resin D	28.00%	82.50%	1	1	1
9	Resin A	23.00%	70.00%	-1.287	0	0
10	Resin E	23.00%	70.00%	+1.287	0	0
11	Resin C	16.57%	70.00%	0	-1.287	0
12	Resin C	29.44%	70.00%	0	+1.287	0
13	Resin C	23.00%	53.91%	0	0	-1.287
14	Resin C	23.00%	86.09%	0	0	+1.287
15	Resin C	23.00%	70.00%	0	0	0
16	Resin C	23.00%	70.00%	0	0	0

[Table 2] Design of experiments for tensile and impact tests

[Table 3] Estimated coefficients in response surface Eq. (1)

Performance	$\beta_0$	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_4$	$\beta_5$	$\beta_6$	$\beta_7$	$\beta_8$	$\beta_9$
Tensile strength	46.07	-0.69	7.66	0.71	-6.36	0.64	0.22	0.10	0.57	-0.42
Failure strain	30.42	-6.39	-0.34	-0.29	-3.28	3.17	1.23	0.30	0.85	0.32
Force reduction	32.68	-1.78	-3.88	-0.72	2.84	-0.24	-0.49	0.06	-0.04	-0.09
Vertical deformation	9.94	-1.15	-2.21	-0.11	0.74	0.56	-0.30	0.57	0.15	0.31

[Table 4] ANOVA table of response function for each performance factor

Performance		Sum of square	Degree of freedom	Root mean square	$F_{o}$	F(a=0.10)	$R^2$
Tensile strength	SSR	902.86	9	100.32	15.336	2.96	0.958
	SSE	39.25	6	6.54	-	-	-
	SST	942.11	15	-	-	-	-
Failure strain	SSR	949.86	9	105.54	3.012	2.96	0.905
	SSE	210.21	6	35.04	-	-	-
	SST	1049.70	15	-	-	-	-
Force reduction	SSR	258.24	9	28.69	13.55	2.96	0.953
	SSE	12.70	6	2.12	-	-	-
	SST	270.94	15	-	-	-	-
Vertical deformation	SSR	79.36	9	8.82	24.64	2.96	0.974
	SSE	2.15	6	0.36	-	-	-
	SST	81.51	15	-	-	-	-

level at least. Here, SSR, SSE and SST are the sum of squares in response, the sum of squares in error and the sum of squares in total, respectively.

Fig. 6 illustrates the typical approximated response surfaces for dynamic performance factor. In Fig. 6, the tensile strength is maximized at the higher resin proportion and the effect of mesh distribution could be negligible; when the resin proportion becomes higher, more and more resin could bind the granules and lead to a higher tensile strength. However, the resin proportion has an adverse effect on the failure strain. Also, the resin and mesh distribution has a similar effect on the force reduction and vertical deformation.



(b) Vertical deformation [Fig. 6] Response surfaces in Resin A

#### 3.2.2 Optimization of performance factors

The goal of this design study was to determine the optimum design variables in the mixing conditions of the

rubber granule layer, which requires the maximization of both the mechanical and dynamic performance. Here, it should be noted that when the impact events occur in the granule layers, the response mechanisms are quite different as mentioned previously. It is, therefore, reasonable to optimize the mechanical and dynamic performance in separate objective functions. Also, the installers have chosen and layered resins considering the efficiency and on-site situations; hence, it is more realistic to optimize the mixing conditions for each resin. Consequently, the objective functions and constraints were given by

Maximize:	$\mu_1  imes \mu_2$	(2)
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Subjected to: $-1.287 \le x_i \le +1.287, i = 1,2,3$	(3)
Maximize: $\mu_1 \times \mu_2$	(4)

Subjected to:  $-1.287 \le x_i \le +1.287, i = 1,2,3$  (5)

in which Eqs. (2) and (3) are the objective function and constraint for mechanical properties, respectively while Eqs. (4) and (5) are for dynamic performance.

The optimization problem was solved by MS-EXCEL solver (generalized reduced gradient approach) [9]. Table 5 shows the optimized design variables and the corresponding expected mechanical and dynamic performance for each polyurethane resin. Regardless of resin types, as the resin proportion increases, the tensile

Design	Results for	mechanical proper	ties	Results for dynamic performance			
Variables	Optimal	Expected prope	rties	Optimal Expected performance		mance	
	variables	Tensile strength	Failure strain	variables	Force reduction	Deformation	
<i>x</i> <sub>1</sub>	Resin A			Resin A			
$x_2$	29.435	0.483 MPa	40.835 %	16.565	44.663 %	1.393 mm	
<i>X</i> 3	53.913			57.225			
<i>x</i> <sub>1</sub>	Resin B			Resin B			
$x_2$	29.435	0.521 MPa	40.948 %	16.565	42.286 %	1.670 mm	
<i>X</i> 3	53.913			57.688			
<i>x</i> <sub>1</sub>	Resin C			Resin C			
$x_2$	29.435	0.576 MPa	37.433 %	16.565	37.642 %	1.394 mm	
<i>X</i> 3	86.088			59.313			
$x_{I}$	Resin D			Resin D			
$x_2$	29.435	0.514 MPa	29.250 %	16.565	38.645 %	1.268 mm	
<i>x</i> <sub>3</sub>	86.088			61.088			
$x_{I}$	Resin E			Resin E			
$x_2$	29.435	0.473 MPa	25.691 %	16.565	43.534 %	1.490 mm	
<i>x</i> <sub>3</sub>	86.088			61.638			

[Table 5] Optimized design variables and expected performance

strength tends to be maximized. The mesh distribution, however, has a somewhat different effect on the mechanical properties. Also, their maximum values are somewhat different for each resin, which may result from the different adhesive characteristics of each resin. But, the dynamic performance exhibits quite different behavior from the mechanical properties; it has almost the same optimum variables for all resin types. It is inferred that the properties of the granule are most important for the dynamic performance while the resin functions simply to hold the granule in place.

From Table 5, the optimal design variables differ with resin type and loading condition, and the the corresponding mechanical and dynamic performances differ also greatly with the resin types. For further understanding these behaviors, the maximum mechanical and dynamic performances are plotted against the resin type as shown in Fig. 7. For convenience, the mechanical and dynamic performances are normalized by their maximum value in each resin type. The tensile strength has a somewhat adverse trend with resin types compared with the failure strain, and the layer with resin C has the most outstanding properties. However, the dynamic performance exhibits different behavior from the mechanical properties; the layer with resin C has the inferior performance, and the higher dynamic performance can be found in the layer with resin B.

Actually, when the engineers settle upon the mixing condition for the rubber granule layer on-site, it is almost impossible to simultaneously maximize the mechanical and dynamic performance. Therefore, they should determine which performance factor is of more importance. And they should also acknowledge that when the optimization problem is solved for any performance, the other performance level will be reduced. For this, decreases in performance factor are calculated and plotted in Fig. 8.

Here  $\mu_{i,app}$  is the approximated factor obtained using the design variables when the optimization is performed for mechanical properties. Also,  $\mu_{i,max}$  is the expected factor listed in Table 5. The dynamic performance is more sensitive to the design variables, leading to higher reductions overall. In contrast, the failure strain is rather increased when it is calculated by the design variables, which are obtained by optimizing for dynamic performance. It is, therefore, desirable to optimize the dynamic performance when the optimal mixing conditions are needed on site.





[Fig. 8] Reductions in performance factor

# 4. CONCLUSIONS

1. For in-plane loading, the adhesive characteristics are the dominating factor to improve the mechanical properties. However, under out-of-plane loading, the resin may play a role only in holding the granules, and the properties of the rubber granules are the important factors determining the dynamic performance

- Based on the design of experiments and the three design variables, response surfaces were constructed to optimize the mixing condition for the mechanical and dynamic performance of the rubber granule layer.
- 3. The optimization problem was formulated and solved separately for each resin, to maximize the mechanical and dynamic performance. The mechanical properties are mainly affected by the proportion and resin type. However, the dynamic performance is more sensitive to the design variables and more important to the performance of the rubber granule layer.
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